

## Homework 6

2. There are  $(10^3 \text{ bit/fr}) / (56 (10^3) \text{ bit s}^{-1}) = (1/56) \text{ s}$  per frame time.

Max throughput  $S$  for pure ALOHA is  $(1/(2e))$  successful transmissions per frame time.

There are  $(1/(2e)) \text{ fr frtm}^{-1} (100 \text{ s}) / ((1/56) \text{ s frtm}^{-1}) = 1030.062$  frames transmitted for each period during which each station may transmit once, so there are maximum

**1030 stations.**

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3. At low load there are few collisions, so we expect the typical frame offering to succeed.

So, for pure ALOHA, because a transmission begins immediately, the delay should equal the time it takes to transmit a frame; i.e., the frame time, call it  $T$ .

For slotted ALOHA, a frame must wait, on average,  $1/2$  the slot time, or  $1/2 T$ , to begin transmission. So the delay under low load for slotted ALOHA is  $(T + 0.5 T) = 1.5 T$ .

Therefore under low load, **pure ALOHA has less delay.**

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6. a. Channel load  $G$  is expected value of (# frames generated / frame time), or  $P(\text{a frame will be generated within one frame time})$ , so

$$G = (1 - 0.1) = \mathbf{0.9}$$

b.  $S = Ge^{-G} = 0.9e^{-0.9} = \mathbf{0.366}$

c. An optimal load for slotted ALOHA is  $G = 1.0$ , with  $S = 0.37$ , so the channel is

**slightly underloaded.**

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21. The time for the signal to travel twice the distance between the cable ends is:

$$2 \text{ km} / (2 (10^5) \text{ km/s}) = 10^{-5} \text{ s}$$

The frame must take at least this long to be transmitted. So,

$$\text{min frame length} = (10^9 \text{ bits/s}) (10^{-5} \text{ s}) = 10^4 \text{ bits} = \mathbf{10 \text{ kb}}$$