

Homework #3 - Chapter 2

Problem 8: (480 x 640) pixel/image (24 bit/pixel) (60 image/s) = 442.368 Mbps is the necessary data transfer rate. Since this is an ideal channel, we use the theoretical limit imposed by Nyquist: For bandwidth H, using 2-level logic, max rate $r = 2 H \log_2(2) = 2 H$.

Thus the required bandwidth is

$$H = (562.368)(10^6) \text{ s}^{-1} (1/2) = \mathbf{221.184 \text{ MHz}}$$

We seek a band of wavelength about 1.3 microns, which corresponds to a band of frequency of width 281.184 MHz. The center frequency is

$$f = c/\lambda = (2.998) (10^8) \text{ m s}^{-1} / (1.3)(10^{-6}) \text{ m} = 2.306154 (10^{14}) \text{ Hz}$$

A band of 221.184 (10⁶) Hz about this frequency, corresponds to a band of

$$B_\lambda = (1.3)(10^{-6}) \text{ m} (221.184)(10^6) \text{ s}^{-1} / (2.306154 (10^{14}) \text{ s}^{-1}) = (1.246834)(10^{-12}) \text{ m}$$

$$B_\lambda = \mathbf{1.2 \times 10^{-6} \text{ microns}}$$

Problem 9: $f_1 = c / \lambda_1 = (2.998) (10^8) \text{ m s}^{-1} / 1(10^{-2}) \text{ m} = 2.998 (10^{10}) \text{ s}^{-1}$

$$f_2 = c / \lambda_2 = (2.998) (10^8) \text{ m s}^{-1} / 5 \text{ m} = 0.5996 (10^8) \text{ s}^{-1}$$

So the range of frequencies is **60 MHz to 30 GHz**

Problem 15: A hand-sketched drawing and some hand-waving were both helpful, but are not reproduced here. Suppose the satellite aligns with the person on the surface at latitude ϕ and the center of Earth, at time t_0 . The satellite will appear to be positioned straight overhead of the observer. Then, as time passes, the satellite will appear to sink toward the horizon and travel east. At time ($t_0 + 6$ hours), the satellite will drop below the horizon in the east. At time ($t_0 + 18$ hours), the satellite will appear above the horizon in the west, and will then rise toward the top of the sky as it travels from west to east. At time ($t_0 + 24$ hours), the satellite will be in the same location it started, and the cycle will continue.